Some properties of eigenvalues and generalized eigenvectors of one boundary-value problem

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Abstract: We investigate one discontinuous boundary value problem which consist of a Sturm-Liouville equation with piecewise continuous potential together with eigenparameter-dependent boundary conditions and supplementary transmission conditions. We establish some spectral properties of the considered problem. In particular it is shown that the generalized eigenfunctions form a Riesz basis of the adequate Hilbert space.

Keywords: Discontinuous boundary value problem, boundary conditions, Riesz Basis

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