

The Coinciding Polygonal Numbers and the Related Arithmetical Properties of Tchebyshev Polynomials

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Abstract: We present an algorithm for identification of all coinciding heptagonal and square numbers. The solution to the corresponding Diophantine equation is in the form of three series of ascending solutions. We also specify arithmetic progressions containing certain linear combinations of values of Tchebyshev polynomials at odd triangle numbers.

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