Error a posteriori estimation for a problem of optimal control of the obstacle

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Abstract: This poster is devoted to a problem of the optimal control of the obstacle represented as follows

(1)
$$\min_{\psi \in U_{ad}} \left\{ \frac{1}{2} \int_{\Omega} \left(\mathcal{T}_g(\psi) - z \right)^2 dx + \int_{\Omega} \left(\nabla \psi \right)^2 dx \right\}$$

subject to:

(2)
$$\forall v \in \mathcal{K}(\psi) : a(y, v - y) + \langle g(y) - f, v - y \rangle \ge 0; y \in \mathcal{K}(\psi)$$

such that

(3)
$$\mathcal{K}(\psi) = \left\{ y \in H_0^1(\Omega); \ y \ge \psi, \ \operatorname{pp dans} \Omega \right\}$$

(4)
$$a(u,v) = \sum_{i=1}^{n} \left(\sum_{j=1}^{n} a_{ij} \int_{\Omega} \frac{\partial u}{\partial x_i} \frac{\partial v}{\partial x_j} dx + b_i \int_{\Omega} v \frac{\partial u}{\partial x_i} dx \right) + \int_{\Omega} cuv dx$$

where $a_{i,j}$, b_i and c in $L^{\infty}(\Omega)$. Moreover, on suppose $a_{i,j} \in \mathcal{C}^{0,1}(\Omega)$ (space of Lipschitz functions continues on Ω) and c non negative, where the form bilinear a(.,.) is continuous and coercive with M et m are respective

Despite the non-differentiability of the $y = \mathcal{T}_g(\varphi)$ application, this type of problem has been widely studied by several authors on a mathematical level (see for example [1,2] but little has been done digitally.

After finite element discretization, and in spite of the non-convex character of this kind of problem, our main goal is to give estimates of the a posterior errors on the state and the control (see for example [2]).

Keywords: Probleme of the obstacle, optimal Control, Penalization

References

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