## A note on hyperbolic differential equations on manifold

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**Abstract:** The well-posedness of nonlocal boundary value problems for partial differential equations of hyperbolic type has been studied extensively (see, e.g. [1–4] and the references therein).

The present abstract investigates the differential equations on smooth closed manifolds and considers the well-posedness of boundary value problem for hyperbolic equations in Hölder spaces. Moreover, it is established new coercivity estimates in various Hölder norms for the solutions of such boundary value problems for hyperbolic equations.

**Keywords:** Differential equations on manifolds, well-posedness, self-adjoint positive definite operator

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