On the number of contractions in the finite full transformation semigroup

Shamsuddeen Habibu¹, Umar Mallam Abdulkarim², Hassan Abubakar Augie³, Abdussamad Tanko Imam⁴

^{1,3} Department of Mathematics, Federal College of Education (Technical), Gusau, Nigeria

Shamsuddeenhabeeb@gmail.com

Augiehassan 55@gmail.com

 2 Department of Mathematical Sciences, Nasarawa State University, Keffi, Nigeria

abdulmallam @yahoo.com

⁴ Department of Mathematical Sciences, Ahmadu Bello University, Zaria, Nigeria

Imam.abdussamad@gmail.com

Abstract: Let $X_n = \{1, 2, 3, ..., n\}$ and T_n be the full transformation semigroup on X_n , that is the semigroup of all full transformation of the set X_n . A transformation α in T_n is said to be a contraction if $|\alpha(x) - \alpha(y)| \le |x-y|$ for all $x, y \in X_n$. The transformation α in T_n is order preserving if $x \le y \Rightarrow \alpha(x) \le \alpha(y)$ for all $x, y \in X_n$. In this paper we denote by CT_n and OCT_n the subsemigroups of T_n consisting respectively of all contraction and order preserving contraction in T_n (number of elements in each of the semigroup) and obtain formulae for the order of the two semigroups.

Keywords: Contraction, semigroup, subsemigroup, order preserving, full transformation